

Calculate the True Mean Bearing of the Line

Calculate forward bearing

Forward bearing at A (cor. of secs. 5, 6, 31 and 3)2: N. $0^{\circ} 00' 00''$ E. + $89^{\circ} 44' 19''$ = **N. $89^{\circ} 44' 19''$ E.**

Calculate angular convergence:

Angular convergence for meridians 6 miles apart at Lat. $47^{\circ} 30'$:

From Table 11: Convergence at 47° = $0^{\circ} 05' 34''$

Convergence at 48° = $0^{\circ} 05' 46''$

Convergence at $47^{\circ} 30'$: $(0^{\circ} 05' 34'' + 0^{\circ} 05' 46'') \div 2 = 0^{\circ} 05' 40''$

$0^{\circ} 05' 40'' = 340''$

$340'' \div 31680.00 \text{ ft. (6 miles)} = 0.010732''$ per ft. of departure

$0.010732'' \times 7960.73 \text{ ft. (1/2 departure of the line)} = 0^{\circ} 1' 25.44''$

Mean bearing: N. $89^{\circ} 44' 19''$ E. (forward bearing) + $0^{\circ} 1' 25.44''$ (correction) = **N. $89^{\circ} 45' 44.44''$ E.**

(The correction is applied clockwise because the bearing is easterly and we are going from forward bearing to true bearing)

Calculate departure of the line

Departure of the line: $\sin 89^{\circ} 44' 19'' \times 15921.62 = \text{E. } \mathbf{15921.45 \text{ ft.}}$

Calculate the single proportion

The record calls for 6 equal 40 ch. segments, therefore: $\text{E. } 15921.45 \div 6 = \mathbf{\text{E. } 2653.58 \text{ ft.}}$

Calculate the forward bearing from A to each of the lost corners

Line A-B:

$\text{E. } 2653.58 \div 2 = 1326.79 \text{ ft. (1/2 the departure of line A-B)}$

$\text{E. } 1326.79 \times 0.010732''$ (angular convergence per ft. of departure) = $0^{\circ} 00' 14.24''$ (angular convergence)

N. $89^{\circ} 45' 44.44''$ E. (mean bearing line A-G) - $0^{\circ} 00' 14.24''$ (angular convergence) = **N. $89^{\circ} 45' 30.24''$ E.**

(We are going from true bearing to forward bearing therefore the correction is applied counterclockwise for easterly lines and clockwise for westerly line. The opposite is true when going from forward bearing to true bearing.)

Distance of line A-B: $2653.58 \text{ ft. (departure of A-B)} \div \sin 89^{\circ} 45' 30.24'' = \mathbf{2653.60 \text{ ft.}}$

At Pt. A the forward bearing and distance to Pt. B on the curve is:

N. $89^{\circ} 45' 30.24''$ E., 2653.60 ft

Coordinates of the proportioned point: **N.10011.19, E.12653.58**

Line A-C:

$\text{E. } 5307.16 \div 2 = 2653.58 \text{ ft. (1/2 the departure of line A-C)}$

$\text{E. } 2653.58 \times 0.010732''$ (angular convergence per ft. of departure) = $0^{\circ} 00' 28.48''$ (angular convergence)

N. $89^{\circ} 45' 44.44''$ E. (mean bearing line A-G) - $0^{\circ} 00' 28.48''$ (angular convergence) = **N. $89^{\circ} 45' 15.96''$ E.**

(We are going from true bearing to forward bearing therefore the correction is applied counterclockwise for easterly lines and clockwise for westerly line. The opposite is true when going from forward bearing to true bearing.)

Distance of line A-C: $5307.16 \text{ ft. (departure of A-C)} \div \sin 89^\circ 45' 15.96'' = \mathbf{5307.21 \text{ ft.}}$

**At Pt. A the forward bearing and distance to Pt. C on the curve is:
N. $89^\circ 45' 15.96''$ E., 5307.21 ft**

Coordinates of the proportioned point: N.10022.75, E.15307.16

Line A-D:

$E.7960.74 \div 2 = 3980.37 \text{ ft. (1/2 the departure of line A-D)}$

$E.3980.37 \times 0.010732'' \text{ (angular convergence per ft. of departure)} = 0^\circ 00' 42.72'' \text{ (angular convergence)}$

$N. 89^\circ 45' 44.44'' \text{ E. (mean bearing line A-G)} - 0^\circ 00' 42.72'' \text{ (angular convergence)} = \mathbf{N. 89^\circ 45' 01.72'' \text{ E.}}$

(We are going from true bearing to forward bearing therefore the correction is applied counterclockwise for easterly lines and clockwise for westerly line. The opposite is true when going from forward bearing to true bearing.)

Distance of line A-D: $7960.74 \text{ ft. (departure of A-D)} \div \sin 89^\circ 45' 01.72'' = \mathbf{7960.81 \text{ ft.}}$

**At Pt. A, the forward bearing and distance to Pt. D on the curve is:
N. $89^\circ 45' 01.72''$ E., 7960.81 ft.**

Coordinates of the proportioned point: N.10034.67, E.17960.74

Line A-E:

$E.10614.32 \div 2 = 5307.16 \text{ ft. (1/2 the departure of line A-E)}$

$E.5307.16 \times 0.010732'' \text{ (angular convergence per ft. of departure)} = 0^\circ 00' 56.96'' \text{ (angular convergence)}$

$N. 89^\circ 45' 44.44'' \text{ E. (mean bearing line A-G)} - 0^\circ 00' 56.96'' \text{ (angular convergence)} = \mathbf{N. 89^\circ 44' 47.48'' \text{ E.}}$

(We are going from true bearing to forward bearing therefore the correction is applied counterclockwise for easterly lines and clockwise for westerly line. The opposite is true when going from forward bearing to true bearing.)

Distance of line A-E: $10614.32 \text{ ft. (departure of A-E)} \div \sin 89^\circ 44' 47.48'' = \mathbf{10614.42 \text{ ft.}}$

**At Pt. A, the forward bearing and distance to Pt. E on the curve is:
N. $89^\circ 44' 47.48''$ E., 10614.42 ft.**

Coordinates of the proportioned point: N.10046.96, E.20614.32

Line A-F:

$E.13267.90 \div 2 = 6633.95 \text{ ft. (1/2 the departure of line A-F)}$

$E.6633.95 \times 0.010732'' \text{ (angular convergence per ft. of departure)} = 0^\circ 01' 11.20'' \text{ (angular convergence)}$

$N. 89^\circ 45' 44.44'' \text{ E. (mean bearing line A-G)} - 0^\circ 01' 11.20'' \text{ (angular convergence)} = \mathbf{N. 89^\circ 44' 33.24'' \text{ E.}}$

(We are going from true bearing to forward bearing therefore the correction is applied counterclockwise for easterly lines and clockwise for westerly line. The opposite is true when going from forward bearing to true bearing.)

Distance of line A-F: $13267.90 \text{ ft. (departure of A-F)} \div \sin 89^\circ 44' 33.24'' = 13268.03 \text{ ft.}$

At Pt. A, the forward bearing and distance to Pt. F on the curve is:
N. $89^\circ 44' 33.24''$ E., 13268.03 ft.

Coordinates of the proportioned point: N.10059.61, E.23267.90

Line A-G:

$E.15921.48 \div 2 = 7960.74 \text{ ft. (1/2 the departure of line A-G)}$

$E.7960.74 \times 0.010732'' \text{ (angular convergence per ft. of departure)} = 0^\circ 01' 25.43'' \text{ (angular convergence)}$

$N. 89^\circ 45' 44.44'' \text{ E. (mean bearing line A-G)} - 0^\circ 01' 25.43'' \text{ (angular convergence)} = \mathbf{N. 89^\circ 44' 19.01'' \text{ E.}}$

(We are going from true bearing to forward bearing therefore the correction is applied counterclockwise for easterly lines and clockwise for westerly line. The opposite is true when going from forward bearing to true bearing.)

Distance of line A-G: $15921.48 \text{ ft. (departure of A-G)} \div \sin 89^\circ 44' 19.01'' = \mathbf{15921.65 \text{ ft.}}$

At Pt. A, the forward bearing and distance to Pt. F on the curve is:

N. $89^\circ 44' 19.01''$ E., 15921.65 ft *(notice this agrees with the measured forward bearing and distance of line A-G. The minor difference in distance is the result of rounding)*

Coordinates of the proportioned point: N.10072.64, E.25921.48